Workshop: Macro Programming with ImageJ

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```java
setBatchMode(true);
while(next()) {
    run("Analyze Image");
}
setBatchMode("exit and display");
```

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Chapter 1

Introduction

In this workshop you will learn how to write and use macros for the automation of image analysis tasks with the public domain software ImageJ\cite{9}.

Ideally you have already used ImageJ before, but you know nothing or very little about programming. If this is not the case you might still find parts of the workshop interesting. If necessary you can discover ImageJ in the same time that you learn the macro programming and if you are already a skilled programmer you can still find information on how to work with ImageJ specific objects.
Chapter 2

Getting Started

In this chapter we will explain what ImageJ macros are, what you can do with them and what limitations they have. In order to be able to write macros we will install FIJI. FIJI[8] stands for "FIJI is Just ImageJ". FIJI is a distribution of ImageJ that comes with a number of extensions (plugins and macros) for biological-image analysis.

2.1 Macros

In ImageJ, macros are scripts, written in the ImageJ-macro language[6], that can be executed by ImageJ and that allow to automatize most of the things that you can do manually with ImageJ. All entries in the ImageJ menus can be called from a macro. Furthermore the macro language provides some basic data types like numbers and strings and basic programming constructs like loops and conditional execution. Finally it provides an interface to ImageJ’s objects and tools like images, files, histograms, regions of interest (roi), the roi-manager, the curve fitting tool, overlays and more.

Macros can run completely without user interaction (in batch mode) or with user interaction. A macro can have a simple user interface that allows to adjust parameter values. Macros can be integrated into ImageJ as ImageJ menu commands or as tool buttons. They can be run from the command line of your operating system or from ImageJ and they can be triggered from events like the opening of a new image in ImageJ. They can even be run from within other software packages like Cellprofiler[5] or KNIME[4].

ImageJ allows the usage of other scripting languages. The standard ImageJ distribution comes with JavaScript as scripting language and FIJI has support for JavaScript, Jython, JRuby, Clojure and BeanShell. What is the difference between these scripting languages and the ImageJ-macro language? Technically the ImageJ macro language is interpreted by ImageJ, while the other languages are either interpreted by a special java program or compiled into java-bytecode that is executed by the java virtual machine. The world macro is an abbre-
viation for macroinstruction. In assembler and other programming languages macroinstructions are used as a shorthand for multiple basic instructions. A pre-processor replaces the macro with the basic instructions. In a similar way ImageJ’s macro language can be thought of as allowing to bundle a number of basic ImageJ commands, give them a name and allow to run them using that name or by a keyboard shortcut. This point of view is supported by the fact that ImageJ macros can be created by recording the menu commands called in an interactive ImageJ session. However it has some elements that go beyond usual macro languages mainly the ability to define functions and to call them recursively, which means that a function can directly or indirectly call itself with eventually modified parameters and the execution repeats until a condition is fulfilled. The main difference is in the complexity. The ImageJ macro language is build to provide enough glue to automatize ImageJ. The scripting languages are general purpose programming languages that can access ImageJ’s application user interface. They are therefore more complex and more difficult to learn. However the minimalism of the macro language comes with a price. Although beginners will easily get started with it, more advanced things might be harder to do. Another problem is the limited re-usability of macros. Since there is no import or include statement for macros, functions must be defined in each macro. The only way to make a function available in multiple macros is to make it available to all macros.

ImageJ allows to write plugins in the java programming language as well. As a difference from macros and scripts these plugins need to be compiled and installed before they can be run.

As a conclusion from the above, the ImageJ macro language is certainly a good choice if you want to automatize an analysis protocol that you can execute manually with ImageJ. If you need to implement complex new image analysis algorithms, scripting languages or plugins might be a better choice.

2.2 Installing Fiji

Download the version of Fiji appropriate for your operating system from http://fiji.sc/Downloads. Unzip the archive file and save the containing folder Fiji.app into a directory for which you have write access. Enter the folder Fiji.app and run the application by double-clicking the program that starts with ImageJ-. By default FIJI will check for updates each time you start it. If updates are available, accept the check and apply the changes.

Figure 2.1: The FIJI launcher window.
2.3 Hello World

We will now write the traditional "Hello World!" example. The idea is that whenever you start to learn a new programming language, you first write a very simple program that outputs the text "Hello World!". This allows you to learn how to edit and run programs in the new language and programming environment.

We will write three different versions. One that does the output in a log-window, another that writes the output on a dialog and a last one that writes the output into a new image.

2.3.1 Hello World using the log-window

Open the macro-editor from the menu Plugins>>New>>Macro or use the keyboard shortcut ctrl+shift+N. The macro-editor will open on a new macro with the name Macro.ijm. The file-extension .ijm stands for imagej macro. In the editor window enter the following command:

```java
print("Hello World!");
```

Listing 1: Hello World using the log-window.

Execute the macro from the menu Run>Run or by pressing ctrl+r. If the log window was closed it will be opened. The text "Hello World!" will be written to the log window each time you run the macro.

![Log window with "Hello World!" messages](image)

Figure 2.2: The "Hello World" message displayed in the log window.

Now let us examine the macro from listing 1 in detail:

- `print` is a built-in function of the ImageJ macro language that allows to write output somewhere. By default the output is written to the log window.
• The brackets separate the name of the function from the argument or the arguments that are passed to the function.

• "Hello World!" is a literal string. A string is a sequence of characters. It is literal because the characters are directly written down. The macro language knows that it is a literal string and not a misspelled command because it is embedded within the " characters.

• The semicolon is necessary to separates commands in a macro (since this macro only has one command it would run without the semicolon at the end).

2.3.2 Hello World using a dialog

Either open the macro editor again from the menu Plugins>>New>>Macro or if it is still open, open a new macro in the editor from the menu File>>New of the editor window. This will open a second tab for the new macro. This time enter the command:

```java
showMessage("Hello World!");
```

Listing 2: Hello World using a dialog.

Run the macro. It will show the "Hello World!" message on a dialog. Note that the dialog is modal. While it is open the execution of the macro is paused and all other windows of ImageJ are unresponsive. This makes sure that the user notices the message before he continues working. You can close the dialog by pressing the "OK" button.

![Figure 2.3: The "Hello World" message displayed on a dialog.](image)

If you want to know more about the print or the showMessage commands, call Help>>Macro Functions... from the ImageJ launcher window. This will open a description of all build in functions of the macro language.

2.3.3 Hello World on an image

Since this workshop is about image analysis, we will now display the "Hello World!" message on an image. We will do this in a way that does not modify
the pixel values of the image, by using an overlay. We will use the example to introduce the macro-recorder and to show how to run single macro commands.

Open an image. ImageJ comes with a number of example images. You can use one of those, for example the "Fluorescent Cells" image. Download it via the menu item File>>Open Samples>>Fluorescent Cells (400K). Open the macro-recorder from Plugins>>Macros>>Record.... Any command you run will be recorded by the macro recorder now, until you close the "Recorder" window. In order to write the text we use the text tool. It is the 9th tool-button on the ImageJ launcher window (the one labelled 'A'). Note that double clicking the button opens a dialog that allows to modify the options of the text tool. Select the text tool, click somewhere in the image and open a rectangular selection. Type in "Hello World!”. When done use Image>>Overlay>>Add Selection... to add the text to an overlay or press ctrl+b. Click somewhere in the image to get rid of the selection and see the effect of adding the text to the overlay. We’re done, now let us create the macro from the recorded commands. On the macro-recorder, press the ‘Create’ button. This will open the macro editor with the list of recorded commands copied into it.

Listing 3: A macro that writes "Hello World!" onto an overlay of an image.

```java
//setTool("text");
setFont("Serif", 40, "antialiased");
setColor("#ffc800");
Overlay.drawString("Hello World!", 126, 128, 0.0);
Overlay.show();
```

Remove the overlay you created when you recorded the macro by using Image>>Overlay>>Remove Overlay. Now run the macro and make sure it reproduces the "Hello World!" message.

Figure 2.4: The "Hello World" message displayed on an overlay of an image.

We will examine the macro step by step again:
1. The line beginning with two slashes is a comment. In this case the macro-recorder added it to record that the text tool has been activated. It uses a comment because the selection of the text tool will not modify the result of the macro. You can remove this line from your macro.

2. `setFont` is a build in function that sets the font for the `drawString` function.

3. `setColor` sets the foreground color. The foreground color will be used by the `drawString` function. However it is used for other purposes as well and it would be a good idea to reset it after the macro. Colors can either be passed by name ("black", "blue", "cyan", etc.) or by a hexadecimal representation of the rgb-values ("#ff0000" is pure red, "#00ff00" pure green, etc.)

4. The `drawString` function of the Overlay takes the string to draw, the location on the image and the angle in which the text will be drawn as input.

5. The `show` function of the Overlay makes the overlay visible on the image.

We will now hide and show the overlay by running single macro commands. Just before the line `Overlay.show()` insert another line and type `Overlay.hide()`. Use the mouse to select the newly inserted line and call Run>>Run selected code from the menu or press shift+ctrl+r. The overlay becomes invisible. Make it visible again by selecting and executing the next line of the macro.

Another way to run single macro commands is to use the Macro interpreter. You can open it from Plugins>>Macros>>Interactive Interpreter... (ctrl+j). Type `Overlay.hide()` and press enter. The command will be executed. Now type `Overlay.show()` and press enter. Note that you can navigate to an existing line in the interpreter and execute it again by pressing ctrl+enter. The ctrl avoids that the enter adds a newline in to the text.

![Interactive Interpreter](image)

Figure 2.5: The macro interpreter allows to run macro commands interactively.
2.4 Excercises

Ex. 1 — Clearing the log window
The command `print("\Clear")` clears the log window. Modify the macro in Listing 1, so that the log window is cleared before the message is written. Run the modified macro multiple times and compare the behaviour of the original macro with the behaviour of the modified version.

Ex. 2 — Message dialog with a title
Did you notice that the message window in figure 2.3 does not have a title? Add a title by modifying Listing 2. In order to give it a title you need to add a parameter to the call of the `showMessage()` command. The title needs to be the first parameter, the text to be displayed the second parameter.

Ex. 3 — Drawing a rectangle on an overlay
Modify the macro in Listing 3! Draw a rectangle around the "Hello World" text onto the overlay! Use the command `Overlay.drawRect(x, y, width, height)`. You need to find the value for x, y, width and height. You can use the menu item `Image>>Overlay>>Remove Overlay` to clean the overlay between different trials.

Ex. 4 — Recording commands
In this exercise you will record a number of commands and apply them to another image. Open an example image. You can use `File>>Open Samples>>Clown (14K)`. Now start the macro recorder and execute the following commands:

- `Process>>Smooth`
- `Process>>Find Edges`
- `Edit>>Invert`

Press the Create button of the macro recorder to create the macro. Now close the image, open another example image, for example `File>>Open Samples>>Bridge (174K)` and run the recorded macro on this image.
2.5 Answers

Answer (Ex. 1) — Clearing the log window

```plaintext
print("\\Clear");
print("Hello World!");
```

Listing 4: In the modified macro the log window is cleared before the text is written.

In the original version of the macro each time you run the macro a line with the output text is added to the log window. In the new version the log window is cleared before the text is written so that the result is a log window with the output text in the first line each time you run the macro.

Answer (Ex. 2) — Message dialog with a title

```plaintext
showMessage("Greetings", "Hello World!");
```

Listing 5: The dialog of the hello world message will now have a title.

Running the macro should produce something similar to figure 2.6.

![Figure 2.6: The dialog now has the title "Greetings".](image)

Answer (Ex. 3) — Drawing a rectangle on an overlay

```plaintext
setFont("Serif", 40, "antialiased");
setColor("#ffc800");
Overlay.drawRect(100,50,300,100);
Overlay.drawString("Hello World!", 126, 128, 0.0);
Overlay.show();
```

Listing 6: A rectangle is drawn around the message.

Running the macro should yield a result similar to figure 2.7.
Figure 2.7: The result of drawing a rectangle around the message.

Answer (Ex. 4) — Recording commands

```plaintext
1 run("Smooth");
2 run("Find Edges");
3 run("Invert");
```

Listing 7: The sequence of recorded commands should look like this.

Figure 2.8 shows the result of applying the recorded macro to the bridge example image.

Figure 2.8: The result image after the recorded macro has been applied to it.
Chapter 3

The ImageJ Macro Language

When talking about programming languages, it is useful to make a distinction between the syntax of the language and its semantics. In a natural language the syntax defines which combinations of symbols form a well-formed sentence. Semantics connects the words of a well-formed sentence to objects and concepts of the real world or of our imagination. In other words the syntax is about the form of sentences and the semantics about the meaning.

Likewise for computer languages the syntax defines what a well-formed program in the language is while the semantics describe the behaviour of the computer when the program is executed. The behaviour can be described in terms of input, inner state of the machine and output [10].

We will not give a formal definition of the syntax of the ImageJ macro language. However we will examine its structure in detail. In the last chapter we already saw that a macro is a list of statements separated by semicolons. We statement can be one of the following:

- a comment
- a literal
- an expression
- an if/else statement
- a looping statement
- a function call
- a declaration of a global variable
- a function definition
- a macro definition
Each item in the above list needs its own definition now. In the suite of this chapter they will be explained informally one by one and for each language construct we will examine its semantics.

Besides of syntax and semantic we will need to discuss how the different language constructs are intended to be used and what pitfalls should be avoided.

3.1 Comments

A comment is a text that the programmer provides for the human reader of the macro. It is ignored when the macro is executed. There are two forms of comments. Comments starting with two slashes extend to the end of the line. Multi-line comments start with /* and end with */.

```java
// a single line comment
/* a multi
 * line comment */
print("\\Clear");
print("Hello World!"); // Another comment
```

Listing 8: The different forms of comments.

There are three or four ways in which comments are used. At the top of each macro file as well as before each macro definition and function definition a comment should explain what the purpose of the code is and how it should be used. Furthermore at the top of each file the author, the copyright holder, the date and the conditions for the usage of the code should be noted. The usage conditions should either tell that the code is in the public domain or under which license the code is distributed.

Another way in which comments are used is to explain parts of the code that are difficult to understand. However, before commenting in this way, you should first try to make the code better so that the comment will not be needed.

Finally you can use comments in the process of debugging a macro, to temporarily deactivate one or multiple commands. You should take care to remove any such comments after the debugging session is finished.
3.2. LITERALS

Listing 9: The ”Hello World” example with comments.

3.2 Literals

Literals in a programming language are values that can be written directly without passing by a function call or an expression, i.e. values that have a literal representation. In the ImageJ Macro Language there are 3 types that have a literal representation:

- numbers (integer or real)
- text (strings)
- truth values (boolean)

The ImageJ macro language internally handles integers and real numbers in the same way and boolean values are represented as 0 and 1. We could therefore simply say that there are only two datatypes with a literal representation, numbers and strings. However, conceptually the distinction between three or four types seems to be more useful. You will find more information about the data types in the next section. Here are some examples of literals:
Let us have a closer look at the literals and the output they produce when running the macro:

1–2 These are the positive integer numbers 7 and 3. Note that negative integer numbers can be written as (-1) where the brackets are not needed in most situations. However, we will not consider this as a literal, but as the unary negation operator applied to 1.
3.3 Expressions, Operators and Datatypes

We can combine values to expressions with the help of operators. The values can be written in literal form or we can use variables as we will see in the next section. When a macro is executed, expressions will be evaluated and replaced by the resulting value. The result can be of the same type as the operands or of a different type.

For example for integer values we have the operator + that will perform the integer addition. We can build and expression 3 + 5; that will be evaluated to 8 when the macro is run.

As an example in which the result type is different from the types of the operands we can take a comparison operator. The expression 3<5 will be evaluated to true.

Operators that have one operand are called unary. Examples are the unary negation operator (-) for numbers or the boolean complement operator (!). Operators that have two operands are called binary operators. Examples are the addition (+) and subtraction (-) operators on numbers. In principal, operators
can have more than two operands, multiple symbols are used in this case to separate the operands. The ImageJ Macro Language only has unary and binary operators.

We will now look at the different datatypes in detail.

### 3.3.1 Numbers

In the ImageJ macro language all numbers are represented the same way. We can consider the numbers as a finite approximation of a finite subset of the real numbers.

#### Numerical Operators

Operations that work on numbers and that yield a number as result are listed in table 3.1.

<table>
<thead>
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<th>Precedence</th>
<th>Result Type</th>
<th>Name</th>
<th>Description</th>
</tr>
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<tr>
<td>-</td>
<td>1</td>
<td>number</td>
<td>negation</td>
<td>unary operator that inverts the sign of the number</td>
</tr>
<tr>
<td>+</td>
<td>3</td>
<td>number</td>
<td>addition</td>
<td>addition of two numbers</td>
</tr>
<tr>
<td>-</td>
<td>3</td>
<td>number</td>
<td>subtraction</td>
<td>subtract operand two from operand one</td>
</tr>
<tr>
<td>*</td>
<td>2</td>
<td>number</td>
<td>multiplication</td>
<td>multiplication of two numbers</td>
</tr>
<tr>
<td>/</td>
<td>2</td>
<td>number</td>
<td>division</td>
<td>divides operand one by operand two</td>
</tr>
<tr>
<td>%</td>
<td>2</td>
<td>number</td>
<td>remainder</td>
<td>the remainder of a division</td>
</tr>
</tbody>
</table>

Table 3.1: Operators that operate on numbers and have numbers as results.

The arithmetical operations should be well known. However, the remainder operator might need some explications. If we have a division \( d = a/b \), then the remainder is the difference between \( a \) and the integer part of the result of the division multiplied with \( b \). Or, written as an equation:

\[
r = a - \lfloor a/b \rfloor \times b. \tag{3.1}
\]

Now we can start to build simple expressions with these operators, before we build more complex expressions involving multiple operators.
3.3. EXPRESSIONS, OPERATORS AND DATATYPES

Listing 12: Simple expressions formed with the negation operator.

```
(-5);
(-(-5));
(-(-(-5)));
(-6.767);
(-2e308);
```

Listing 13: The output produced by listing 12.

```
5
5
-5
-6.767
-Infinity
```

1-4 An even number of negations of a positive number will give a positive result and an odd number of negation a negative result.

5 The biggest number representable in the 64bit double precision is around $10^{308}$. $2 * 10^{308}$ is bigger than the biggest representable number and is therefore considered as Infinity. The negation operator applied to Infinity gives -Infinity.

Listing 14: Simple expressions formed with the addition and the negation operator.

```
5 + 3;
3.56 + 2.45;
(-3 + -5);
(-3 + 5);
1e308 + 1e307;
1e308 + 1e308;
```
Listing 15: The output produced by listing 14.

The result in line 5 of listing 14 is a big number that can still be represented, while the result in line 6 is bigger than the biggest representable number and is interpreted as \texttt{Infinity}.

We skip examples for subtraction and multiplication. You can try them yourself. However, we will have a look at division and remainder.

```
8
6.01
-8
2
1.1000E308
\texttt{Infinity}
```

Listing 16: Simple expressions formed with the division and multiplication operator.

```
8 / 3;
8 / 2;
0.642 / 0.123;
8 / 0;
(8 / 0 * -2)
```

Listing 17: The output produced by listing 16.

Line 4 contains a division by zero. The result is defined as \texttt{Infinity}. In line 5 the result of the division by zero is multiplied by -2 with evaluates to -\texttt{Infinity}.

Listing 18 shows some examples for the remainder operation. It is usually used for integer arithmetic, however using equation 3.1 it can be applied to real numbers as well. Note that the remainder operation can be used to test whether an integer number is even or odd. This is exactly the case if the remainder of the division by 2 is zero. More generally an integer \( n \) is divisible by the number \( d \) if \( n \% d = 0 \).
3.3. EXPRESSIONS, OPERATORS AND DATATYPES

```
8 % 2;
8 % 3;
8.5 % 0.5;
8.5 % 0.8;
(-3 % 2);
0.1 % 10;
```

Listing 18: Simple expressions formed with the remainder and negation operator.

```
0
2
0
0.5
-1
0.1
```

Listing 19: The output produced by listing 18.

1. The integer part of 8 divided by 2 is 4. 4 multiplied by 2 is eight. Eight minus eight is zero.

2. The integer part of 8 divided by 3 is 2. 3 multiplied by 2 is six. Eight minus six is two.

3-5 Apply equation 3.1 to verify the output.

6. The integer part of 0.1 divided by 10 is 0. 10 multiplied by 0 is 0. 0.1 minus 0 is 0.1.

**Special Values**

We already saw the special values *Infinity* and *-Infinity*. There is one more special value that is used when the result of an operation or function is undefined. The value used for an undefined result is *NaN* which stands for "Not a Number". In contrast to *Infinity* and *-Infinity*, *NaN* has a literal representation. However, the macro interpreter will not show the *NaN* in the log window. You have to explicitly print it with the `print` command.

Using only operations the only way to produce a *NaN* value from a calculation is by dividing a zero value by a zero value. As we saw before, a non-zero value divided by zero yields *Infinity*. According to [3], zero divided by zero should result in the *NaN* value, which is the case for the ImageJ Macro Language.

You can create all three special values using the built-in macro function `parseFloat()`.
print(0/0);
print(NaN);
print(parseFloat("NaN"));
parseFloat("Infinity");
parseFloat("-Infinity");

Listing 20: Examples of special values.

NaN
NaN
NaN
Infinity
-Infinity


Internal Representation

Before we look at how numbers are internally represented we will shortly explain how to use number representations with different bases. Our usual number system uses the base 10. This means we use 10 digits from 0 to 9 and when we write a number like 1234 we interpret it as \(1 \times 10^3 + 2 \times 10^2 + 3 \times 10^1 + 4 \times 10^0\).

We can use the same principle with any base we want and when the base is bigger than 10 we use letters for the missing digits (A=10, B=11, C=12, ...).

The two bases interesting for us here are base 2 and base 16 or the binary and hexadecimal number representations. In the binary case we use the digits 0 and 1. The number 1234\(_{10}\) in the decimal system becomes 10011010010\(_2\) in the binary system and 4D2\(_{16}\) in the hexadecimal system. Let us check this by converting back to decimal:

\[
\begin{align*}
1 \times 2^{10} + 0 \times 2^9 + 0 \times 2^8 + 1 \times 2^7 + 1 \times 2^6 + 0 \times 2^5 \\
+ 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0
&= 1024 + 128 + 64 + 16 + 2 \\
&= 1234
\end{align*}
\]

\[
4 \times 16^2 + 13 \times 16^1 + 2 \times 16^0 = 4 \times 256 + 13 \times 16 + 2 \times 1 = 1024 + 224 + 2 = 1234
\]

We will now have a look at how the numbers are presented by the computer internally. The ImageJ Macro Language uses the datatype double of the java programming language. The type double implements the 64 bit floating point
format called "binary64" that is described in the IEEE norm 754 [3]. It is important to understand the representation of numbers because it has an influence on the results of calculations and comparisons.

The representation needs to be able to represent fractional parts of numbers and a range of numbers as large as possible. The floating point representation does this by allowing to represent numbers with smaller distances for small numbers while the distances for representable numbers are bigger for bigger numbers. The representation uses 64 bits. 1 bit is used to represent the sign that tells us whether the number is positive or negative. 11 bits are used to encode an exponent and 52 bits are used to represent the fractional part of the number.

The representation of a number in the floating point format is therefore a chain of 64 binary digits (ones and zeros) that are interpreted as a real value as given by equation 3.4.

\[
(-1)^{sign}(1.b_{51}b_{50}...b_0)2 \times 2^{e-1023} \tag{3.4}
\]

Note that we can write the 64 binary digits more comfortably as 16 hexadecimal digits, where the first 3 encode the sign and the exponent and the remaining 13 the fraction.

However there are some special definitions:

1. 0000000000000000_{16} is defined as minus zero and 8000000000000000_{16} as plus zero.
2. if the exponent is zero and the fraction is not zero the number is a sub-normal and interpreted as:

\[
(-1)^{sign}(0.b_{51}b_{50}...b_0)2 \times 2^{1-1023} \tag{3.5}
\]

3. 7FF000000000000_{16} is defined as Infinity and FFF000000000000_{16} as minus Infinity
4. if the exponent has all ones in the binary representation and the fraction is not zero the encoded value is \textit{NaN}.

The smallest representable numbers in normalized form are those that have a one in the exponent and all zero in the fraction which evaluates to:

\[
\pm 2^{-1022} \approx \pm 2.22507 \times 10^{-308} \tag{3.6}
\]
CHAPTER 3. THE IMAGEJ MACRO LANGUAGE

The biggest possible finite numbers are those with the value 2046 in the exponent and all ones in the fraction which gives:

\[ \pm (1 - 2^{-53}) \times 2^{1024} \approx \pm 1.79769 \times 10^{308} \]  

(3.7)

The gap between two representable numbers depends on the exponent. Here are some examples:

- For the exponent 1023 we get the actual exponent 0. The possible range of representable numbers is from 1 to approximately 2. The gap between to neighbouring numbers is approximately $2^{2045} e^{-16}$.

- For the exponent 1076 we get the actual exponent 53. The range is from $9007199254740992$ to $18014398509481982$ with a gap of 2 between representable numbers.

For the above two paragraph see also [11] and [12].

When working with floating point numbers you should be aware that most values can not be represented exactly, which can sometimes give unexpected results. Try to evaluate $0.3 - 0.2 - 0.1$ in the macro editor. The result is $-2.7756 \times 10^{-17}$. We did not introduce comparison operations yet. However considering the above it should be clear that you should not use equality or inequality operators with floating point numbers. Instead you should test if the difference between two values is reasonably small. The expression $(0.3 - 0.2 - 0.1 == 0)$ would evaluate to `false`. However considering that we gave the input numbers with one digit after the decimal point, indicating a precision of one tenth, the value $-2.7756 \times 10^{-17}$ is as close to zero as one could reasonably wish for. We should have therefore used an expression in the form of $(0.3 - 0.2 - 0.1 < 0.01)$.

Calculations and Precedence

The operators in table 3.1 have different precedence values. Operations with smaller precedence value are applied before operations with bigger precedence value, when an expression is evaluated. The operator precedence values reflect the usual multiplication before addition convention. You can change the order in which expressions are evaluated by using brackets. Subexpressions in brackets are evaluated first. Expressions in brackets can include brackets in which case the expressions in the innermost brackets are evaluated first. Listing 22 shows some examples.

```
1 (-1 + 3);
2 (- (1 + 3));
3 2 * 3 + 5;
4 (2 + 3) * 5;
```

Listing 22: Examples for operator precedences.
3.3. EXPRESSIONS, OPERATORS AND DATATYPES

1-2 In line 1 the negation is executed first and the result is 2. In line 2 the addition is executed first and then the negation, leading to the result $-4$.

3-4 Because of the operator precedence the multiplication is executed first in line 3. The result is 17. In line 4 the addition is executed first and the result is 25.

3.3.2 Strings

Strings represent text. Besides of the comparison operations there is only one operator defined on strings. The operator has the symbol + which stands in this case for the concatenation of strings. The concatenation means that the second string is appended to the first one, so that the result is one string that begins with the first string, followed by the second string. As long as we only have string literals this is not very interesting. However as soon as we will use variables the situation will be different. The concatenation of strings is one of the most important operation in the ImageJ Macro Language. It will for example be needed to construct file names and paths and to construct parameters that are passed to commands or build-in functions. Although there is only one operator on strings, there are a number of build-in functions that we will discuss later. These allow for example to find and to replace substrings in strings.

To make it easier to represent the quote characters ‘’ and ‘, a string literal can be embedded in either the double quotes or the single quotes. Some characters preceded by a backslash (\) have a special meaning and are called escape sequences. We already saw the newline (\n) and the tabulator (\t). The tabulator is not interpreted by the log-window but it can be useful when working with tables. Other useful escape sequences are (\’), (\") and (\\). Besides of these the numerical ASCII code [2] in octal form can be used, \040 is for example the octal code for the space character (32 in decimal notation).

```
1 "Hello" + " " + "World" + "!";
2 "Hello \"World\"!";
3 'Hello "World"!';
4 '\n inserts a newline';
5 "\110\145\154\157\041";
```

Listing 23: Examples for string literals, the concatenation operator and escape sequences.
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Listing 24: The output produced by listing 23.

3.3.3 Booleans

Operators that operate on boolean values are the complement (!), the conjunction operator or logical and (&&) and the disjunction operator or logical or (||). The complement has the precedence one just like the numerical negation and the two other boolean operators have the precedence 5 so that when combining comparison operators with boolean operators and numerical operators the numerical operators are executed first, than the comparisons and at the end the boolean operators.

The negation of false is true and the negation of true is false. The result of the boolean and is one when both arguments are one and zero in all other cases and the boolean or is zero when both arguments are zero and one in all other cases. One use of the boolean operations is to combine different comparisons in a condition. Conditions will be needed for the conditional execution of code in if-statements and loops.

Listing 25: The boolean operations not, and and or.

Each table that maps the different combinations of input values false and true or 0 and 1 of the operands to a result value 0 or 1 defines a boolean operator. If we keep the order of the values for the operands fix, we can define an operation simply by giving the four different result values. And would for
example be given by 0001 and or by 0111. There are 16 different possibilities for the four results with the two values 0 and 1. Each defines a different binary boolean operator. Some are rather trivial like 0000 and 1111. An exclusive or (xor) that is true when exactly one of its operands is true would be given by 0110. Note that all the 16 different binary boolean operations can be expressed by only using `and`, `or` and `not`. `and`, `or` and `not` form a functionally complete set of boolean operators. In fact `not` and `and` or `not` and `or` alone do already form a complete set. And even the single operations `nand` given by 1110 and `nor` given by 1000 form each a complete set on its own.

If a and b are the parameters than the xor operation can be expressed by the expression `(!a && b) || (a && !b)`. You can prove this by putting in the different combinations of possible values and comparing the resulting truth table with that of the xor operation.

<table>
<thead>
<tr>
<th>Combination</th>
<th>Expression</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>false</code> and <code>false</code></td>
<td>`(!false &amp;&amp; false)</td>
<td></td>
</tr>
<tr>
<td><code>false</code> and <code>true</code></td>
<td>`(!false &amp;&amp; true)</td>
<td></td>
</tr>
<tr>
<td><code>true</code> and <code>false</code></td>
<td>`(!true &amp;&amp; false)</td>
<td></td>
</tr>
<tr>
<td><code>true</code> and <code>true</code></td>
<td>`(!true &amp;&amp; true)</td>
<td></td>
</tr>
</tbody>
</table>

Listing 26: The boolean operations xor expressed with and, or and not.

Given the truth table of an operation you can find the equivalent expression with `and`, `or` and `not` systematically in the following way. For each row in the result column that contains a one build an expression by negating the operands if they are zero and by not negating them if they are one. Combine the operands using `and` and the sub-expressions for the rows by using `or`. For example the truth table for xor is one for 01 which gives the sub-expression `(!a && b)`. The only other one is for the row 10 with gives the sub-expression `(!true && !true))`. Now the two sub-expressions need to be combined by or which gives `((!a && b) || (true && !(true)))`.

Another useful property is the duality of `and` and `or`. This means if you have an expression containing only `and` and `not` you can obtain an equivalent expression containing only `or` and `not` by replacing every `and` with `or` if you negate each operand and the result of the operation.

\[
\text{a} \&\& \text{b} = \neg(\neg\text{a} \mid\mid \neg\text{b}) \tag{3.8}
\]

and

\[
\text{a} \mid\mid \text{b} = \neg(\neg\text{a} \&\& \neg\text{b}) \tag{3.9}
\]
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Listing 27: The duality of and and or.

### 3.3.4 Numbers as Bit-Strings

There is a number of operations that work on the internal binary representation of the integer part of numbers.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Precedence</th>
<th>Result Type</th>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>~</td>
<td>1</td>
<td>number</td>
<td>bitwise complement</td>
<td>unary operator that changes each 0 to 1 and each 1 to 0</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>(bitwise or)</td>
<td>only zero if both bits are zero</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>bitwise exclusive or</td>
<td>one is exactly one bit is one</td>
</tr>
<tr>
<td>&amp;</td>
<td>2</td>
<td>number</td>
<td>bitwise and</td>
<td>one if both bits are one</td>
</tr>
<tr>
<td>&lt;&lt;</td>
<td>2</td>
<td>number</td>
<td>left shift</td>
<td>shifts the bits of the first operand a number of places give by the second operand to the left</td>
</tr>
<tr>
<td>&gt;&gt;</td>
<td>2</td>
<td>number</td>
<td>right shift</td>
<td>shifts the bits of the first operand a number of places give by the second operand to the right</td>
</tr>
</tbody>
</table>

Table 3.2: Operators that operate on the binary representation of the integer part of numbers.

These operations work on the binary representation of integer numbers in java. Note that in the ImageJ Macro Language all numbers are represented as
3.3. EXPRESSIONS, OPERATORS AND DATATYPES

floating point numbers. However when you use the above operations the integer part of the number is converted internally to integer. To fully understand how they work we need to know how integer values are represented in java.

Two’s complement representation of integer values

Integer values use 32 bits or four bytes in java and can therefore encode \(2^{32} = 4294967296\) different values. Since the 32 bits are long to write, each of the 4 bytes is often written as a two digit hexadecimal number. However to demonstrate the principle we will use just 3 bits. We could of course just use all three bits to binary encode the numbers from 0 to 7. But then we could not represent negative numbers. So we could reserve the leftmost bit to represent the sign with 0 indicating a positive number and 1 a negative number. This is called the signed magnitude representation. It has two disadvantages. First there are two representations for 0 and second the binary arithmetic is not straightforward, since case distinctions depending on the sign must be made. A better representation is the one’s complement. The positive numbers are represented as before. A negative number is build from its positive counterpart by applying the bitwise complement operation. This results in the encodings in table 3.3. Calculations using the one’s complement are simpler. The binary numbers can for example be added in the usual way, only when a carry at the leftmost position occurs it has to be added back at the rightmost position. However there are still two representations for zero.

<table>
<thead>
<tr>
<th>decimal</th>
<th>binary signed magnitude</th>
<th>binary one’s complement</th>
</tr>
</thead>
<tbody>
<tr>
<td>-3</td>
<td>111</td>
<td>100</td>
</tr>
<tr>
<td>-2</td>
<td>110</td>
<td>101</td>
</tr>
<tr>
<td>-1</td>
<td>101</td>
<td>110</td>
</tr>
<tr>
<td>-0</td>
<td>100</td>
<td>111</td>
</tr>
<tr>
<td>+0</td>
<td>000</td>
<td>000</td>
</tr>
<tr>
<td>+1</td>
<td>001</td>
<td>001</td>
</tr>
<tr>
<td>+2</td>
<td>010</td>
<td>010</td>
</tr>
<tr>
<td>+3</td>
<td>011</td>
<td>011</td>
</tr>
</tbody>
</table>

Table 3.3: Signed magnitude representation and one’s complement with 3 bits.

We can get simpler binary arithmetic and unique representations by using the two’s complement. The positive numbers are still encoded as before. The negative counterpart of a positive number is created by building the one’s complement and adding one to the result.
### Bitwise operations

The bitwise complement operation changes each bit in the two’s complement representation of the number from 0 to 1 or from 1 to 0. For example the bitwise complement of 3 is -4. The binary representation of 3 is 011. Inverting each bit yields 100, which encodes -4 in two’s complement representation. Of course our real integer representation uses 32 bits. Note that the bitwise complement of a number \(x\) is \(-x - 1\) if the numbers are represented in two’s complement as is the case here.

The bitwise or will calculate the logical or for each position in the representation of the two numbers. For example: \((-3 | 3)\) gives -1. The binary representations of -3 and 3 are 101 and 011. The bitwise or results in 111 which is the two’s complement representation of -1.

For the exclusive or the result is one if exactly one of the bits is one. \((-3 \oplus 3)\) gives -2, since the resulting representation is 110.

The representation of the result of the bitwise and will have a one at each position at which the representations of both operands have a one. For example: \(3 \& -2\) gives 2. The binary representation of 3 is 011. The representation of -2 is 110. The result of the bitwise and is 010 which encodes 2.

The shift operations move the bits \(n\) positions to the left or to the right. When shifting to the right the highest bit is preserved, when shifting to the left zeros are filled in for the missing values. In the binary representation each digit signifies a power of two. Shifting by \(n\) positions is therefore equivalent to multiplying or dividing (integer division) by \(2^n\). \(256 >> 2\) results in 64 and \(7 << 3\) gives 56.

Sometimes the different bytes of a number are used to encode independent values. This is for example the case for the setPixel\((x,y,v)\) and getPixel\((x,y)\) build-in functions of ImageJ, that in case of RGB images use one single number for an RGB-color value. The bitwise-operations can then be used to retrieve and set the independent parts easily. The rightmost byte (eight bits) encodes the blue value, the next one to the left the green value and the one before this one the red value. The leftmost byte is unused.
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0xFFA900; // color value that encodes a shade of orange

(0xFFA900>>16) & 0xFF; // red
(0xFFA900>>8) & 0xFF; // green
0xFFA900 & 0xFF; // blue

0 | (169<<8) | (255<<16); // create composite value from components

setColorForegroundColor(0xFFA900);

Listing 28: Encoding and decoding of rgb-components in one integer value with the help of bit-operations.

### 3.3.5 Comparison Operations

The comparison operations are defined for all basic datatypes: numbers, booleans and strings. The available operations are less than (<), less than or equal (<=), greater than (>), greater than or equal (>=), equal (==), not equal (!=). Note that the comparison operations have the precedence 4, so that they are evaluated after calculations and before the boolean operations.

(false < true); 1
(true <= true); 1
(7>5); 1
(0.123 < 0.12300000001); 1
(NaN != NaN); 1
("a"<"b"); 1
("fox"<"horse"); 1
("yes"=="yes"); 1

Listing 29: Examples of comparisons.

Note line 5 in listing 29. NaN is not equal to NaN. The IEEE 754[3] specifies:

"All numeric operations with NaN as an operand produce NaN as a result. As has already been described, NaN is unordered, so a numeric comparison operation involving one or two NaNs returns false and any != comparison involving NaN returns true, including x!=x when x is NaN".
3.4 Variables and Assignments

Only working with literal values will not take us very far. We need to write down the same expression each time we want to evaluate it for different values. The solution to this are variables. Variables are an important concept in programming. A variable has an identifier (the name of the variable) and a value that has been assigned to the variable with the help of an assignment operator. Variables can be used in expressions in the same way as literals. Variables allow us to generalize and to write expressions independent from the concrete values for which they will be evaluated.

The identifier of a variable must only contain letters, digits and the underscore ("_") character. It must not begin with a digit. Identifiers are case-sensitive, meaning that for example the lower-case letter "x" will be considered a different variable from the upper-case letter "X".

Before a variable can be used in an expression it must be defined by assigning it a value. This is done with the help of the assignment operator (=). At the left side of the assignment must be a variable and at the right side an expression. The expression can contain variables itself and even the same variable as on the left side if it had already been defined before. When the assignment expression is evaluated, the variables on the right side are replaced by their values before the expression on the right side is evaluated. The result is then assigned to the variable on the left side.

```
1 radius = 11.25;
2 circumference = 2 * PI * radius;
3 area = PI * radius * radius;
4 print("radius:", radius, "circumference:", circumference, "area:", area);
```

Listing 30: Calculation of the area and circumference of a circle with the help of variables. Note that PI is not a variable, but a build-in constant.

```
1 radius: 7.25 circumference: 45.5531 area: 165.13
2 radius: 9.25 circumference: 58.1195 area: 268.8025
3 radius: 11.25 circumference: 70.6858 area: 397.6078
```

Listing 31: Output of listing 30 after changing the radius and running the script multiple times.

It is important to remember that assignment statements with a variable on the right side, assign the value of the right-hand variable to the variable on the
left side as long as basic datatypes are used. They do not create a reference to the right hand variable. This will be different for arrays as we will see later.

```java
balanceA = 1000;
balanceB = balanceA;
balanceB = balanceB + 500;
print("balance A: ", balanceA, "balance B: ", balanceB);
```

Listing 32: The output of the macro is "balance A: 1000 balance B: 1500". Note that balanceA has not been changed when balanceB has been modified.

There is a number of operators that works on variables. We already saw the assignment operator that assigns a value to a variable. As a shortcut for expressions that contain the same variable on the right and on the left side of the assignment there are the operators +=, −=, *= and /=. a+ = 2 is for example a shortcut for a = a + 2, etc.

Furthermore there are the pre and post increment and decrement operators that increment and decrement the value of a variable either before the evaluation of the expression or afterwards.

```java
a = 5;
b = a++ + 3;
c = 5;
d = ++c + 3
print("b:", b, "a:", a); b: 8 a: 6
print("d:", d, "c:", c); d: 9 c: 6
```

Listing 33: The post- and pre- increment operations.
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<table>
<thead>
<tr>
<th>Operator</th>
<th>Precedence</th>
<th>Result Type</th>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>++</td>
<td>1</td>
<td>number</td>
<td>pre- or postincrement</td>
<td>unary operator that adds one to the value of the variable either before the evaluation of the containing expression (preincrement) or afterwards (postincrement)</td>
</tr>
<tr>
<td>−−</td>
<td>1</td>
<td>number</td>
<td>pre- or postdecrement</td>
<td>unary operator that subtracts one from the value of the variable either before the evaluation of the containing expression (predecrement) or afterwards (postdecrement)</td>
</tr>
<tr>
<td>+=</td>
<td>6</td>
<td>number</td>
<td>assignment with addition</td>
<td>add the value on the right hand of the expression to the variable</td>
</tr>
<tr>
<td>−=</td>
<td>6</td>
<td>number</td>
<td>assignment with subtraction</td>
<td>subtract the value on the right hand of the expression from the variable</td>
</tr>
<tr>
<td>*=</td>
<td>6</td>
<td>number</td>
<td>assignment with multiplication</td>
<td>multiply the variable with the value on the right hand of the expression</td>
</tr>
<tr>
<td>/=</td>
<td>6</td>
<td>number</td>
<td>assignment with division</td>
<td>divide the variable by the value on the right hand of the expression</td>
</tr>
</tbody>
</table>

Table 3.5: Operators on variables.

3.4.1 Automatic type conversion

When using the + operator a number can sometimes be automatically converted into a string. This allows to easily construct messages which contain the numerical values of variables. It works when the first operand is a string. If the first operand is a number the second operand is expected to be a number as well and an error will occur.
3.4. VARIABLES AND ASSIGNMENTS

1 \( r = 6.4; \)
2 \( \text{message} = "radius: \ r + \ "cm"; \)
3 \( \text{print(message);} \)
4 \( \text{message} = \text{toString}(r) + \ "cm is the radius"; \)
5 \( \text{print(message);} \)
6 \( \text{message} = "" + r + \ "cm is the radius"; \)
7 \( \text{print(message);} \)

Listing 34: A number is automatically converted into a string when the first operand of the + operator is a string.

3.4.2 Arrays

Arrays are lists of values. In the ImageJ Macro Language the different elements in an array can be of different types. When an array is created it is usually assigned to a variable. An element of the array is read or changed by using an index. The first index is zero and the last index of an array with the length \( l \) is \( l - 1 \).

1 \( \text{primeNumbers} = \text{newArray}(3, 5, 7, 11, 13, 17, 19, 23); \)
2 \( \text{print(primeNumbers[0]);} \)
3 \( \text{print(primeNumbers[primeNumbers.length-1]);} \)
4 \( \text{options} = \text{newArray}(34, \text{true}, "Huang"); \)
5 \( \text{print("threshold value:", options[0]);} \)
6 \( \text{print("dark background:", options[1]);} \)
7 \( \text{print("threshold method:", options[2]);} \)

Listing 35: Two examples of arrays.

Note that arrays are assigned to variables by reference not by value. This means when you have assigned an array to multiple variables, the same array is modified via each variable.

1 \( \text{labels} = \text{newArray("one", "TOO", "three", "four");} \)
2 \( \text{correctLabels} = \text{labels;} \)
3 \( \text{correctLabels[1]} = "two"; \)
4 \( \text{print(correctLabels[1]);} \) two
5 \( \text{print(labels[1]);} \) two

Listing 36: Arrays are assigned by reference.

Arrays can either be created by listing the containing values or by giving
the size of the array. In the second case all elements of the array are initialized with the value 0.

```java
a = newArray(3);
p
```  

Listing 37: Creation of an "empty" array with a given size.

### 3.5 Conditional code execution

A program must be able to react differently depending on the input values or its current internal state. This can be achieved by the if/then/else statement. In the ImageJ Macro Language it has the form shown in Listing 38.

```java
if (condition) {
    list of statements 1
} else {
    list of statements 2
}
```

Listing 38: The form of the if/then/else statement

The condition must evaluate to a boolean value. If the condition is true, the statements in the first block enclosed in curly brackets is executed, otherwise the statements in the else–block are executed. The else-part of the statement is optional and can be omitted.

The then–block and the else–block can contain other if statements, however you should avoid this as far as possible, since programs with nested if-statements are difficult to understand. Note furthermore that when variables are defined in a then–block or else–block, they will only be defined in the following program, if the execution passed by the corresponding block. You should only define variables within a then- or else-block if it is exclusively used within that block, otherwise you should define the variable outside the if-statement (you can then use it within).
3.5. CONDITIONAL CODE EXECUTION

```java
a = getNumber("Enter a number: ", 13);
if (a%2==0) {
    print(a + " is even");
}
else {
    print(a + " is odd");
}
```

Listing 39: Simple example of the if/then/else statement.

Listing 39 shows a simple example. The build-in function `getNumber` is used to get a number `a` from the user. The condition of the if-statement tests if `a` is even by using the modulo operator. `a` is even if `a` modulo 2 is zero. In this case the first block is executed. In this example the list of statements in the block consists of only one statement, which prints out the message "a is even". If the condition evaluates to false, i.e. if `a` modulo 2 is different from zero, the else-block is executed. It prints out the message "a is odd". Note that when a block contains only a single statement the curly brackets can be omitted. However this is not advisable, since it can lead to errors when modifying the code later.

Listing 40 shows an other example. This time the curly brackets have been omitted.

```java
a = getNumber("Enter a number", -3);
if (a<0)
    result = -a;
else
    result = a;
print("abs(" + a + ")=" + result);
```

Listing 40: Another example of a simple if-statement.

This example calculates and displays the absolute value of the entered number. If `a` is smaller than zero the result is the negation of `a` and therefore positive, otherwise the result is `a`.

We can use the if-statement to calculate the maximum of two numbers `a` and `b`. If `a` is larger than or equal to `b` the result is `a`, otherwise the result is `b`. The corresponding code is shown in Listing 41.
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1 a = 10;
2 b = 4;
3 if (a>=b)
4     result = a;
5 else
6     result = b;
7 print("max(\"a\", \"b\")=\" + result);

Listing 41: Calculation of the maximum of two numbers.

Listing 42 shows a more complex example of an if-statement. This time the code contains multiple if-statements. The else-parts have been omitted. The then-blocks contain more than one statement and one of the if-statements is nested, i.e. its then-block contains another if-statement.

waitForUser;
shiftPressed = isKeyDown("shift");
altPressed = isKeyDown("alt");
message = "keys pressed: ";
counter = 0;
if (shiftPressed) {
    message = message + "SHIFT";
counter++;
}
if (altPressed) {
    if (counter>0) message = message + ", ";
    message = message + "ALT";
counter++;
}
if (counter==0) message = message + " NONE";
print(message);

Listing 42: Using the if-statement to test which modifier keys are pressed.

The macro will display which of the modifier keys SHIFT and ALT are pressed. The waitForUser-command pauses the execution of the macro until the user clicks the ok-button on the dialog that the command opens. This gives you the possibility to press and hold down the modifier keys. The isKeyDown build-in function will answer true if the specified key is pressed. At the end a message indicating that either none of the keys, the shift-key, the alt-key or both have been pressed. The nested if, in the if-statement that tests if the alt-key is pressed, allows to add a comma in the case that both keys are pressed. Note that it would be bad style to write the condition as "if (shiftPressed==true)
...". The variable is already boolean and it is unnecessary to compare it to true or false.

In Listing 43 the variable b is defined in the then-block of the if-statement. Running the macro will produce an error. Since a is zero the execution does not pass into the then-block of the first if-statement and b will be undefined in the condition of the second if-statement. To correct the macro b should be defined at the top of the macro for example with the expression b = 0;

```java
1 a = 0;
2 if (a>0) {
3     b=2;
4 }
5 if (b>1) {
6     c=3;
7 }
8 print(c);
```

Listing 43: The example will produce an error because b will be undefined in line 5.

### 3.6 Loops

A loop allows to repeatedly execute a code block. A condition is evaluated for each iteration of the loop and decides when the loop finishes. In image processing, loops can for example be used to load each image from a given folder or to apply an operation to each pixel of an image. In the ImageJ Macro Language there are three different forms of loops: the for-loop, the while-loop and the do-while-loop.

#### 3.6.1 The for–loop

The for-loop is preferably used when the number of iterations is known from the start. It has the form shown in Listing 44.

```java
for (initialization; condition; increment) {
    list of statements
}
```

Listing 44: The form of a for-loop.

The initialization is executed one time at the beginning, before the loop is entered. It is normally used to initialize the counter variable of the loop. The condition is evaluated before each iteration of the loop. If it evaluates to true
the loop is entered, otherwise the execution of the code continues after the body of the loop. The condition usually tests if the counter variable of the loop has reached a specific value. The increment is executed after each iteration of the loop. It is usually used to modify the counter variable of the loop.

Listing 45 shows a basic example of a for-loop. The macro prints the numbers from one to ten.

```plaintext
for (i=1; i<11; i++) {
    print(i);
}
```

Listing 45: The loop prints the numbers from one to ten.

Listing 46 prints out the even numbers from two to ten. It increments the counter variable of the loop by two in the increment. Let us see how this is executed. The first time the execution reaches the loop, \( i \) is initialized to 2. The condition is executed and since \( 2 < 11 \) evaluates to true, the body of the loop is entered. The value of \( i \) which is currently 2 is printed. The increment is executed and adds 2 to the current value of \( i \) so that \( i \) has now the value 4. Now the condition is executed with \( i = 4 \) and evaluates to true. The execution enters the body of the loop, and so on. After 6 iterations \( i \) reaches the value 12. This time the condition evaluates to false and the execution continues after the body of the loop.

```plaintext
for (i=2; i<11; i+=2) {
    print(i);
}
```

Listing 46: The loop prints the even numbers from two to ten.

In the next example the counter variable of the loop starts with a high number and counts down to 2. This macro calculates the \( n \)th factorial, i.e. the multiplication of the numbers from one to \( n \). Remember that \( i -- \) means \( i = i - 1 \) and \( factorial* = i \) stands for \( factorial = factorial * i \). In the first iteration \( factorial \) is one and \( i \) five. \( factorial \) becomes five. In the next iteration \( factorial \) is five and \( i \) four. And so on. In the last iteration \( i \) is two while \( factorial \) is \( 5 * 4 * 3 * 2 = 120 \).
3.6. LOOPS

Listing 47: Calculation of the nth factorial.

Loops are often used to process each element of a given list of elements. This can for example be the numbers in an array or the files and sub-folders in a folder. When iterating over the elements of an array, you must remember that the index of the first element is zero. If the array contains \( l \) elements, the index of the last element is \( l - 1 \). If \texttt{numbers} is a variable containing an array, \texttt{numbers.length} returns the number of elements in the array \texttt{numbers}.

The example in Listing 48 replaces each element of the array by the square of the element. The build-in function \texttt{Array.print} is used to print all elements of the array at the end.

Listing 48: Squaring each element in an array.

The next example will print the names of files and sub-folders in your home folder, each in a separate line. The macro uses the build-in function \texttt{getDirectory} with the parameter "\texttt{home}". This answers the path to the user’s home folder. The path is then passed to the function \texttt{getFileList}, which will return an array of the names of files and folders in the given folder. The loop iterates over this array and prints each element.

Listing 49: Printing the files and folders in the user’s home folder.
Note that each part `initialization`, `condition` and `increment` can be missing. If the condition is missing the only way to exit the loop is to exit the whole macro with an error by using the `exit` command.

```java
i=2;
for (; ; ) {
  print(i);
  if (i>=10) exit("FINISHED");
  i+=2;
}
print("EXECUTION WILL NEVER PASS HERE");
```

Listing 50: A loop with an empty `initialization`, `condition` and `increment`.

The for-loop in Listing 50 prints out the even numbers from two to ten. When ten is reached the macro is stopped with an error. Since the `condition` of the loop is empty, this is the only way to exit the loop.

The `initialization` and the `increment` can use other variables as the counter of the loop and the `condition` can be any expression that evaluates to a boolean value. However you should normally avoid to use such unusual style, because it can easily be misinterpreted by others or yourself when you come back to the code later.

Listing 51 implements a simple number guessing game. The game is over, either when the player guessed the right number or when he made ten wrong guesses. A for-loop is used since the maximal number of trials is known beforehand, however the condition checks not only the counter variable but also a flag that indicates if the player has won the game.

```java
number = floor(100 * random) + 1;
guess = getNumber("Guess my number between 1 and 100: ", 50);
won = false;
for(i=1; ((i<10) && !won); i++) {
  if (guess==number) {
    showMessage("you won!");
    won = true;
  } else {
    if (number<guess) message = "my number is smaller, try again: ";
    else message = "my number is bigger, try again: ";
    guess = getNumber(message, guess);
  }
}
if (!won) showMessage("I won!");
```

Listing 51: A simple number guessing game.
3.6. LOOPS

We will now iterate over all pixels of a two-dimensional image. To demonstrate this, we will create a new empty image and then create a pattern on it, by setting each pixel to a value, depending on its coordinates in the image. Since we can easily access the width and the height of the image and since we can specify the pixel coordinates by their $x$ and $y$ positions, the easiest way is to use a nested for-loop. The outer loop iterates over one dimension and the inner-loop over the other. Note that if the outer loop runs from 0 to $N - 1$ and the inner loop from 0 to $M - 1$, the body of the inner loop is executed $N \times M$ times. It can therefore be important to not do unnecessary things in the body of the inner loop.

```c
newImage("pattern", "8-bit", 255, 255, 1);
width = getWidth();
height = getHeight();
for(x=0; x<width; x++) {
    for(y=0; y<height; y++) {
        setPixel(x, y, x*y % 255);
    }
}
```

Listing 52: Looping over the pixels of an image.

Listing 52 will produce an image similar to that in Figure 3.2.

![Image of pattern created by Listing 52](image)

Figure 3.2: The pattern created by the example macro in Listing 52.

Instead of creating a pattern, we can modify the pixel values of an existing image. Listing 53 shows an example that uses a nested for-loop to invert the contrast of an 8-bit image, by replacing each pixel value $v$ by $255 - v$. You need to open an 8-bit image before running this macro. You can for example use the boats-example-image from the menu File>Open Samples>Boats (356K).
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width = getWidth();
height = getHeight();
for(x=0; x<width; x++) {
    for(y=0; y<height; y++) {
        value = getPixel(x, y);
        setPixel(x, y, 255-value);
    }
}

Listing 53: Using a nested for-loop to invert the contrast of an 8-bit image.

By changing the position of an object in an image in a loop we can create an animation. The example in Listing 54 creates a region of interest in the upper left corner of the image and moves it along the diagonal until it leaves the image in the lower right corner. Depending on the speed of your machine, you might need to change the argument of the wait command. The wait command will cause ImageJ to pause for the given time in milliseconds before the execution continues. Without it the macro might run to fast to see the animation.

newImage("animation", "8-bit", 800, 800, 1);
makeOval(0,0,20,20);
Roi.setFillColor("red");
for(i=0; i<800; i++) {
    Roi.move(i, i);
    wait(20);
}

Listing 54: Using a for-loop to create an animation.

3.6.2 The while–loop

The while-loop has the form shown in Listing 55. Before the body of the loop is entered, the condition is executed. If it evaluates to true, execution continues in the body of the loop. When the execution reaches the end of the body of the loop, the condition is evaluated again. If it still evaluates to true the body of the loop is entered again, otherwise the execution continues after the body of the loop.

while(condition) {
    list of statements
}

Listing 55: The form of the while-loop.
It is clear that while- and for-loop are equivalent in the sense that for every while-loop there is a for-loop that can simulate it and vice versa. To simulate a while-loop by a for loop it is sufficient to use the condition of the while-loop in the for-loop and to leave the initialization and increment empty. A for-loop can be simulated by a while-loop by putting the initialization directly before the loop and the increment as the last statement in the body of the loop.

While-loops are preferably used when the number of times the loop will run is not known at the beginning. This is for example the case when calculating an iterative approximation of a function. We can for example calculate the square root of a given number using Newton’s method. According to Newton’s method, if we have an initial approximation $A$ for the value of the square root of $N$, we get a better approximation by dividing $N$ by $A$, adding $A$ to the result and dividing the result by 2.

$$A_{i+1} = \frac{1}{2} \cdot \left( \frac{N}{A_i} + A_i \right)$$  \hspace{1cm} (3.10)

We do not know beforehand how many iterations we will need until the result is good enough. However since we can easily calculate the square we can test if $A^2$ is sufficiently close to $N$ and in this case we know that we can stop iterating.

```
1 input = 121;
2 guess = 1;
3 nr_iterations = 0;
4 while(abs((guess*guess) - input) > 0.000001) {
5     guess = 0.5 * ((input / guess) + guess);
6 }
7 print(guess);
```

Listing 56: Calculation of the square root using Newton’s method.

Another example is to calculate the number of times a given number can be divided by 2 using integer division until the result is 1. For example:

$$9 = 2 \times 4 + 1$$ \hspace{1cm} (3.11)
$$4 = 2 \times 2 + 0$$ \hspace{1cm} (3.12)
$$2 = 2 \times 1 + 0$$ \hspace{1cm} (3.13)

So the answer for the input nine is three. Note that this corresponds to the integer part of the logarithm to the basis 2. Here again we do not know beforehand how many iteration are needed.
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```java
n = 128;
counter = 0;
while(n>1) {
    n = floor(n / 2);
counter++;
}
print(counter);
```

Listing 57: Calculation of the integer part of the logarithmus dualis.

As a last example we will present a random walk that stops when it reaches the border of the image. Imagine an object in the middle of the image. In each step the object moves a given distance in a random direction, either up, down, left or right and leaves a trace while moving. Since the direction is random in each step, we can not know after how many iterations the object will reach the border of the image.

```java
newImage("random-walk", "8-bit", 800, 800, 1);
x = 400;
y = 400;
makeOval(x,y,20,20);
moveTo(x,y);
Roi.setFillColor("green");
while(x>=0 && x<800 && y>=0 && y<800) {
    x = x + 10 * round((2 * random) -1);
y = y + 10 * round((2 * random) -1);
    Roi.move(x, y);
    lineTo(x,y);
    wait(10);
}
```

Listing 58: A random walk that stops when the border of the image is reached.

Note that, the way we implemented the random walk, the object can actually stay at its current coordinates for some steps, since the increment for the coordinates can be zero. You can see an example of a random walk in Figure 3.3.

### 3.6.3 The do–while–loop

The do–while–loop works similar as the while–loop. However in this case the condition is evaluated after each iteration and not before. This means that other as for the while–loop the body of the do–while–loop is guaranteed to be executed at least once. The form of the do–while–loop is shown in Listing 59.
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Figure 3.3: The image created by the random walk in Listing 58.

```java
do {
    list of statements
} while (condition);
```

Listing 59: The form of the do–while–loop.

Note that the do–while–loop can be simulated by a while–loop, by copying
the content of the body of the loop one time before the beginning of the loop.
In the example in Listing 60 the user is asked for a number between zero and
one. The loop continues until the user enters a number fulfilling this condition.

```java
do {
    n = getNumber("Enter a number between 0 and 1", 0.5);
} while (n<0 || n>1);
print("number:", n);
```

Listing 60: Using the do–while–loop to obtain valid input.

3.7 User–defined functions

In the ImageJ Macro Language you can define your own functions. A function is
a block of code that has a name and a number of arguments. When the function
is called, the arguments are replaced by the values in the call and the body of
the function is executed. A function can have a return value. If this is the case
the function call can be used on the right–side of an assignment statement or as
the parameter of another function call. Listing 61 shows the form of a function
definition.
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In Listing 47 we used a for-loop to calculate the factorial of a number \( n \). Remember that the factorial of the number \( n \) is the product of the numbers from 1 to \( n \). Imagine that the calculation of factorials is needed at different places in your macro. You could of course copy the code from Listing 47 to each place where the factorial needs to be calculated. However this approach has multiple problems:

- Imagine you made an error in the code that calculates the factorial, you will have to correct it for each copy
- Imagine you find a better way to calculate factorials that works faster, if you want your macro to fully benefit, you have to change all copies again.
- At all the places where you want to calculate factorials you find the code that describes how to calculate factorials. This will make your macro hard to read and understand.

So it is much better to define and use a function that calculates factorials. Listing 62 shows how this can be done.

```java
function factorial(n) {
    result = 1;
    for (i=n; i>1; i--) {
        result *= i;
    }
    return(result);
}
```

A function does not need to have a return value. Instead of returning a calculated value, it can modify an inner state, for example an image or a results table in ImageJ. The example in Listing 63 creates a circular region of interest (roi) with a given radius around the center of the current image.

```java
print(factorial(5));
print(factorial(factorial(5)));
result = factorial(3);
print(result);

function factorial(n) {
    result = 1;
    for (i=n; i>1; i--) {
        result *= i;
    }
    return(result);
}
```

Listing 62: A function that calculates the factorial of a number and its usage.
3.7. USER–DEFINED FUNCTIONS

```javascript
function makeCircleAroundCenter(radius) {
    makeOval((getWidth() - radius) / 2, (getHeight() - radius) / 2, radius, radius);
    Roi.setStrokeWidth(7);
}
```

Listing 63: A function that draws a circle around the center of the image.

The function `makeCircleAroundCenter` cannot be used in an assignment statements or as the parameter of another function since it does not have a return value. However it still represents a useful abstraction and does some useful work by creating a roi on the current image.

### 3.7.1 Variable scope and global variables

The scope of a variable is the part of the code in which the variable can be accessed. It starts with the definition of the variable and goes to the end of the block in which the variable is defined. It is visible in sub-blocks as in the bodies of loops and if-statements, but not in the bodies of function declarations. Function declarations have their own variable scope.

```javascript
a = "outer";
show();
print(a);
function show() {
    a = "inner";
    print(a);
}
```

Listing 64: This macro prints "inner" followed by "outer".

The macro in Listing 64 assigns the value "outer" to the variable `a` in the outer scope of the macro. It calls the function `show`. In the function `show` another variable `a` is defined and the value "inner" is assigned to it. However the function has its own variable scope and the assignment in the function does not affect the variable `a` in the outer scope. Therefore the function prints "inner" and returns. Now the value of the variable `a` in the outer scope, "outer" is printed.

The situation is different when using global variables. Global variables are declared on the outer level of a macro, using the keyword `var`. The scope of a global variable is the whole program in which it is declared global, including all
function and macro bodies. Global variables allow the different functions and macros in a file to communicate.

If we declare the variable \( a \) in Listing 64 global, the assignment in the function–body will change the value of the global variable \( a \) and the macro will output "inner" twice.

```java
var a = "outer";
show();
print(a);
function show() {
    a = "inner";
    print(a);
}
```

Listing 65: Now that \( a \) is a global variable, the output is two times "inner".

Another problem can occur when the parameter of a function has the same name as a global variable. In this case the parameter will not modify the value of the global variable, however within the function that has this parameter the global variable with the same name is not accessible any more. This is called variable shadowing.

```java
a = "outer";
show("inner");
print(a);
function show(a) {
    print(a);
}
```

Listing 66: An example of variable shadowing.

Here are some rules that you should consider to avoid problems when working with global variables:

- Avoid to use global variables when they are not really useful
- Declare global variables at the top of the file.
- Make sure that global variables are recognized as such by using a naming convention. Let global variables begin with an underscore, use only uppercase letters and separate words with underscores. For example: 

  `_INPUT_FOLDER_.` Never let other variables begin with an underscore. You could of course use other prefixes to indicate global variables, but as soon as letters are involved it will make the code less readable.

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3.7. USER-DEFINED FUNCTIONS

We will now demonstrate the use of global variables in a small example. We will develop a turtle-graphics [7] macro. Imagine a turtle that sits at the coordinates \(x, y\) on the image. It is headed into a direction given by the angle \(\alpha\). You can give the following commands to the turtle:

**forward** \(n\) The turtle moves \(n\) units forward in the direction depending on the current angle.

**right** \(a\) The turtle turns \(a\) degrees to the right.

**left** \(a\) The turtle turns \(a\) degrees to the left.

There are usually some more commands but we do not need them right now. The turtle-graphics system is used to teach programming to children. We will implement the three commands above as functions and the current coordinates and the current angle will be global variables, so all functions can access them. Besides these, we will use two more global variables, the radius with which the ROI, that represents the turtle is drawn and a delay, that allows to slow down the movement of the turtle so that we can follow it. Besides of the three functions that represent the three commands above, we will implement one more function that initializes the turtle, so that in the beginning it is in the middle of the image.

```javascript
var _CURRENT_X = 0;
var _CURRENT_Y = 0;
var _CURRENT_ANGLE = 0;
var _RADIUS = 20;
var _DELAY = 400;

function initializeTurtle() {
  _CURRENT_X = getWidth() / 2;
  _CURRENT_Y = getHeight() / 2;
  moveTo(_CURRENT_X, _CURRENT_Y);
  makeOval(_CURRENT_X - (_RADIUS / 2),
            _CURRENT_Y - (_RADIUS / 2),
            _RADIUS, _RADIUS);
  Roi.setFillColor("green");
}
```

Listing 67: Global variables that represent the location and orientation of the turtle and the initialization.

The initialization modifies the global variables _CURRENT_X and _CURRENT_Y. It sets them to the coordinates of the center of the image. It then moves the current drawing position to this point. It draws the turtle as a ROI with the radius given by the global variable _RADIUS around the center of the image and sets the fill-color of the turtle to green.
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```
function forward(step) {
    _CURRENT_X += step * cos(_CURRENT_ANGLE * PI / 180);
    _CURRENT_Y += step * sin(_CURRENT_ANGLE * PI / 180);
    lineTo(_CURRENT_X, _CURRENT_Y);
    Roi.move(_CURRENT_X - (_RADIUS / 2), _CURRENT_Y - (_RADIUS / 2));
    wait(_DELAY);
}

function right(delta) {
    _CURRENT_ANGLE += delta % 360;
}

function left(delta) {
    _CURRENT_ANGLE -= delta % 360;
}
```

Listing 68: Implementation of the three turtle–graphics commands.

The `right` and `left` functions are very simple. They just increment or decrement the current angle of the turtle by the given amount. They use modulo 360, since after 360 degrees the turtle has completely turned around one time. The `forward` function calculates the new position depending on the length the turtle shall advance and its present orientation. It draws a line from the current drawing position to the new position of the turtle. Note that the `draw` function updates the current drawing position, so that we do not have to do it ourselves. Now the ROI representing the turtle is moved to the new position and the macro pauses for the given delay in order to let us follow the movement.

Now let us create a new image and give some commands to the turtle.

```
run("Select All");
run("Clear");
initializeTurtle();
forward(100);
right(90);
forward(50);
left(90);
forward(100);
```

Listing 69: Usage of the turtle–graphics commands.

The Listing 69 should produce an image similar to Figure 3.4. We will come back to the turtle–graphics later when we talk about recursion.
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Figure 3.4: Example output of turtle-graphics.

### 3.7.2 Parameter passing by value and by reference

In the ImageJ Macro Language, parameters that have a basic type, i.e. numbers and strings are passed by value and arrays by reference. This means that when you call `factorial(n)` with a variable `n` defined in the outer scope, the value of this variable will not be modified. However, when you pass a variable containing an array into a function and the function modifies the elements of the array the elements of the array in the outer variable are modified. This is why the output of Listing 70 is "5 25" and the output of Listing 71 is "1, 4, 9" for `a` and for `b`.

```java
1 a = 5;
2 b = squareValue(a);
3 println(a, b);
4 function squareValue(a) {
5 a = a * a;
6 return a;
7 }
```

Listing 70: The output is "5 25"; The `a` in the outer context is not modified by the commands in the function.

```java
1 a = newArray(1,2,3);
2 b = squareList(a);
3 Array.println(a);
4 Array.println(b);
5 function squareList(a) {
6 for (i=0; i<a.length; i++)
7     a[i] = a[i] * a[i];
8 return a;
9 }
```

Listing 71: The output is two times "1, 4, 9"; The `a` in the outer context is modified by the commands in the function.
Bibliography